

### INTRODUCTION

Maps of the global solar photospheric magnetic field play an important role in solar and heliospheric physics. Routine measurements of the surface field occur only along the Sun-Earth line. Flux transport models attempt to mitigate this limitation by modeling the surface evolution of the field.

Here we present the first public release of the High-Performance Flux Transport code (HipFT), which implements advection, diffusion, and data assimilation over the solar surface. It can produce multiple realizations of the evolving flux, allowing uncertainty quantification. The code is modular, so users can easily add custom flow, diffusion, source, and data assimilation models.

HipFT is the computational core of the upcoming Open Source Flux Transport (OFT) model, which will be a complete system for generating full-Sun magnetograms through acquiring & processing observational data, generating realistic convective flows, and running the flux transport model.

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### MODEL

$B_r(t, \theta, \phi)$  Surface radial magnetic field

$$\frac{\partial B_r}{\partial t} = -\nabla_s \cdot (\mathbf{v} B_r) + \nabla_s \cdot (\nu \nabla_s B_r) + D + S$$

$$\nabla_s \cdot (\nu(\theta, \phi) \nabla_s B_r) = \frac{1}{\sin \theta} \frac{\partial}{\partial \theta} \left( \nu(\theta, \phi) \sin \theta \frac{\partial B_r}{\partial \theta} \right) + \frac{1}{\sin^2 \theta} \frac{\partial}{\partial \phi} \left( \nu(\theta, \phi) \frac{\partial B_r}{\partial \phi} \right)$$

$$\nabla_s \cdot (B_r \mathbf{v}_s(x, t)) = \frac{1}{\sin \theta} \frac{\partial}{\partial \theta} (\sin \theta B_r v_\theta) + \frac{1}{\sin \theta} \frac{\partial}{\partial \phi} (B_r v_\phi)$$

$\mathbf{v}_s = (v_\theta, v_\phi)$  Flow velocities  
 $D$  Data assimilation  
 $S$  Sources (e.g. emerging flux)  
 $\nu$  Diffusion coefficient

**GRID**  
 Non-uniform, logically rectangular, with field and velocities staggered

# HipFT v1.0

## An Open Source High-Performance Flux Transport Model

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github.com/  
predsci/hipft

### NUMERICAL METHODS

**SPATIAL METHODS**  
**FLOW:** 1<sup>st</sup>-order Upwind  
 4<sup>th</sup>-order WENO3 [Smit et al. (2005)]

**DIFFUSION:** 2<sup>nd</sup>-order central finite difference

**TEMPORAL METHODS:**  
 Flow and diffusion are 2<sup>nd</sup>-order  
 Strang operator-split [McLachla et al. (2003)]

**FLOW:** 3<sup>rd</sup>-order RK3TVD [Gottlieb et al. (1998)]

**DIFFUSION:** 2<sup>nd</sup>-order Runge-Kutta-Gegenbauer [Skaras et al. (2021)]

### VALIDATION

$u(\theta, \phi, t) = 1000 e^{-12t} \left( Y_0^2(\theta, \phi) + \sqrt{\frac{11}{11}} Y_5^2(\theta, \phi) \right)$  End Time: 28 days  
 $\nu = 500 \text{ km}^2/\text{s}$

**DIFFUSION ONLY** (CV/RMSD) vs  $\Delta\theta, \Delta\phi$

**DIFFUSION+ADVECTION** (CV/RMSD) vs  $t_{\text{diff}} = \Omega \sin \theta$

Combine with rigid rotation with constant angular velocity in phi over 1 full rotation  
 $\Omega = 1.8076 \dots \text{ km/s}$

### CODE & PARALLELISM

- Written in Fortran 2023
- Fortran standard parallelism (do concurrent) for multi-core CPU or GPU
- OpenMP Target for GPU data management
- MPI is used to parallelize realizations across multiple CPUs/GPUs

```

do concurrent (k=2:npm-1, j=2:ntm-1)
  y(j,k) = coef(j,k,1)*x(j, k-1) &
    + coef(j,k,2)*x(j-1,k) &
    + coef(j,k,3)*x(j, k) &
    + coef(j,k,4)*x(j+1,k) &
    + coef(j,k,5)*x(j, k+1)
enddo
    
```

### PERFORMANCE

**Test:** 28-day run at 1024x512 with analytic flow models and diffusion. Eight realizations spanning various levels of diffusion and flow attenuation

**In-house workstation:**  
 EPYC 7702P 64-core CPU  
 Four RTX 2080Ti GPUs

Wait clock time (minutes) vs GPU count (1xGPU, 2xGPU, 4xGPU)

### DATA ASSIMILATION

Acquire data (e.g. HMI M720s LOS through JSOC drms py package)

Convert line-of-sight field into radial field:  
 $B_r = B_{\text{los}} / \mu$

Map to Carrington frame with resolution 10240 x 5120 to avoid under-sampling

Reduce size with flux-preserving integral binning:

Set quality weights:  
 $\mu = \cos \theta_d \in [0, 1]$   
 $\theta_d$  is the center to limb angle

Use weights with power and cutoff parameters to assimilate data into HipFT:

$$F = \mu^{\alpha} \quad \mu < \mu_{\text{lim}}$$

$$F = 0 \quad \text{o.w.}$$

$$D = \frac{1}{\Delta t} (F B_{r,d} - F B_r)$$

### FLOW MODELS

**Differential Rotation**  $v_\phi(\theta) = [d_0 + d_2 \cos^2 \theta + d_4 \cos^4 \theta] r \sin \theta$

**Meridional Flows**  $v_\theta(\theta) = [-m_1 \cos \theta - m_3 \cos^3 \theta - m_5 \cos^5 \theta] \sin \theta$

**Flow Attenuation** (reduces flow velocities in active regions)  
 $v \rightarrow v \left[ 1.0 - \tanh \left( \frac{|B_r|}{B_0} \right) \right]$

**Super Granular Convective Flows** [Hathaway et al. (2010,2015)]

### MULTIPLE REALIZATIONS

- Uncertainty quantification is very important when there are variations in observed data and model parameters
- To facilitate this, HipFT has been designed to compute many realizations of maps spanning several user-defined data assimilation and model parameters
- MPI is used to spread the realizations evenly across compute units (GPUs or CPU-sockets) to allow the efficient computation of a large number of realizations in a single run

**Polar Average Field (within 30 degrees of poles)**

### COMPARISON TO OTHER FLUX TRANSPORT MODELS

- Maps from FT models are processed by interpolating to 300x150 resolution, flux balancing, and smoothing
- Note some models apply scaling factors to the HMI data

### EXAMPLE PRODUCTION RUN

Initial map from AFT model, HMI data assimilation (1-hour cadence), ConFlow (1CR) and analytic flows with 500G attenuation, diffusion of 175 km<sup>2</sup>/s

Runtime on an NVIDIA RTX 2080Ti GPU: **13:00:00**

Butterfly Diagram (1CR average)